

# Chapter 22 Magnetism

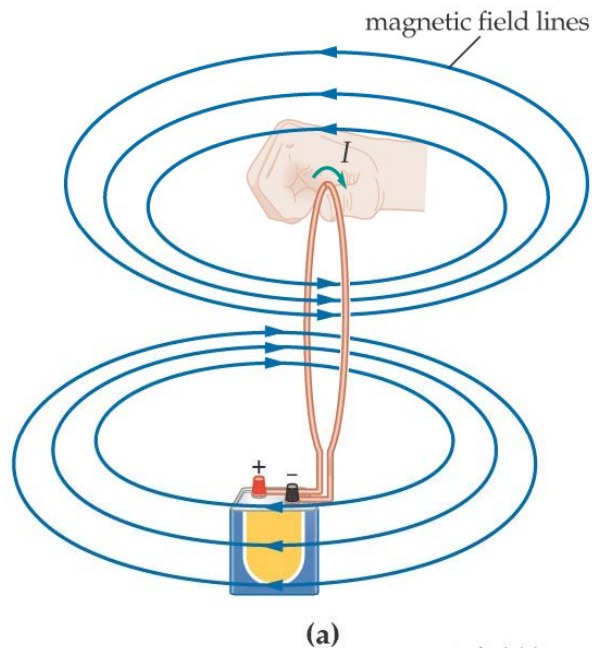
## Outline

- 22-1 The Magnetic Field
- 22-2 The Magnetic Force on Moving Charges
- 22-3 The Motion of Charges Particles in Magnetic Field
- 22-4 The Magnetic Force Exert on a Current-Carrying Wire
- 22-5 Loops of Current and Magnetic Torque
- 22-6 Electric Current, Magnetic Fields, and Ampère's Law
- 22-7 Electric Loops and Solenoid

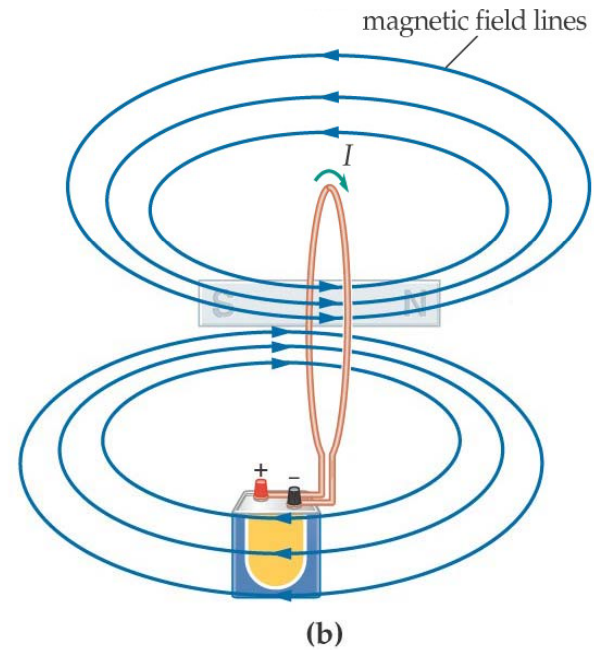
## 22-7 Electric Loops and Solenoid

### Current Loop

A Current-carrying wire can produce magnetic field.

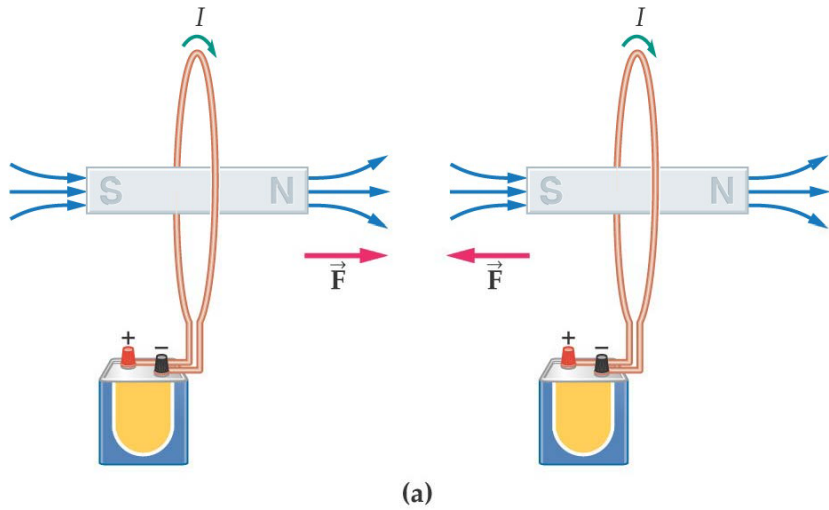


**Figure 22-25a**  
**The Magnetic Field of a**  
**Current Loop**

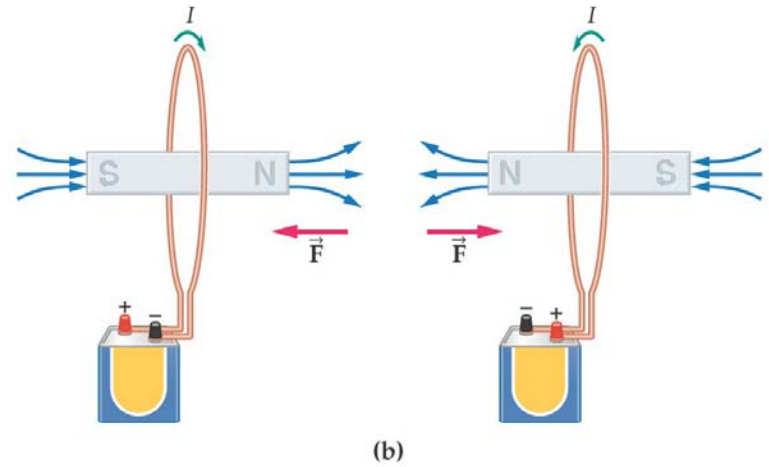


**Figure 22-25b**  
**The Magnetic Field of a**  
**Current Loop**

**Figure 22-26a**  
**Magnetic Forces**  
**Between Current Loops**



**Figure 22-26b**  
**Magnetic Forces Between**  
**Current Loops**



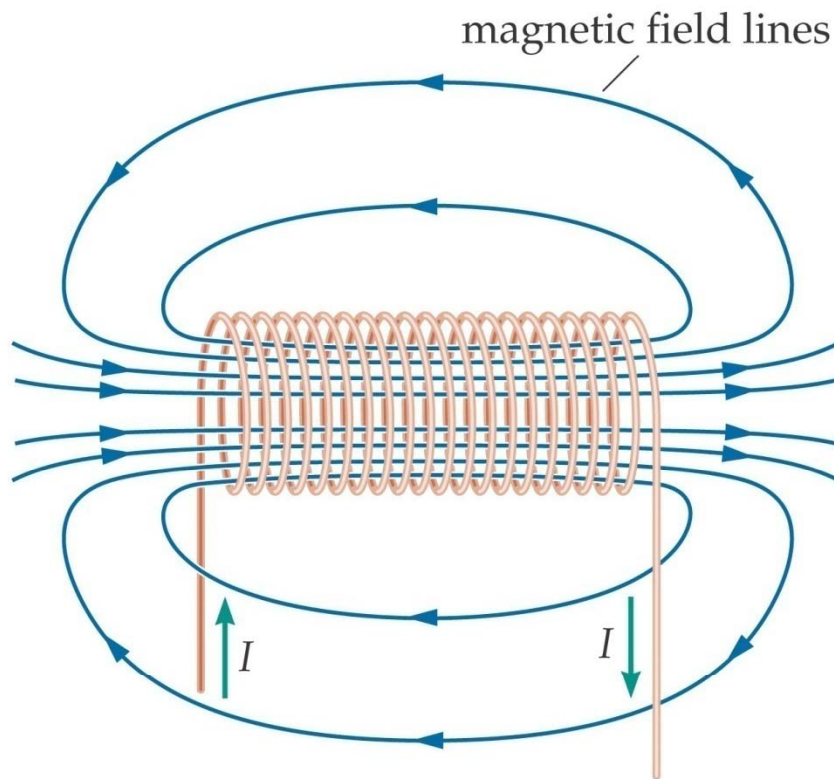
The magnetic field produced by *a circular loop of N turns*, radius R, and current varies at different locations. **At the loop center**, it can be expressed as

$$B = \frac{N\mu_0 I}{2R} \quad (22-11)$$

## Solenoid

A Solenoid is an electric device in which a long wire wound into a succession of closely spaced loops with the geometry of a helix.

A solenoid carrying a current can produce an intense, nearly uniform magnetic field inside the loops, as shown in the figure.



*Outside the loop, the magnetic field is so weak compared with that the inside, so it is zero for the outside (idealization case).*

**Figure 22-27**  
**The Solenoid**

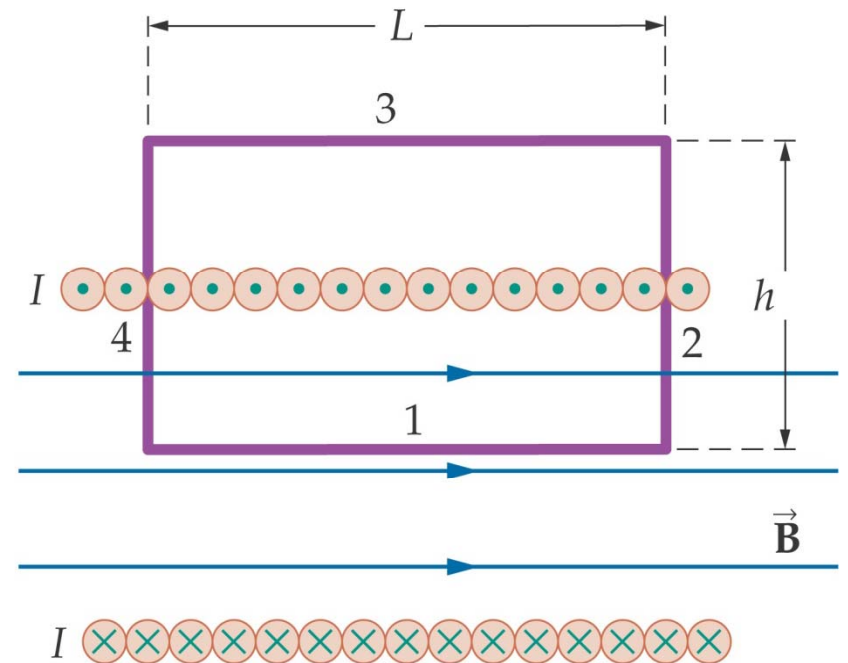
## Deriving magnetic field

Applying the Ampère's Law to the loop (shown in the figure), we have

$$\begin{aligned}\sum B_{\parallel} \Delta L &= \sum_{\text{side1}} B_{\parallel} \Delta L + \sum_{\text{side2}} B_{\parallel} \Delta L + \sum_{\text{side3}} B_{\parallel} \Delta L + \sum_{\text{side4}} B_{\parallel} \Delta L \\ &= BL + 0 + 0 + 0 = BL\end{aligned}$$

The current enclosed by the rectangular circuit is  $NI$ , where  $N$  is the number of the loops. So we have

$$BL = \mu_0 NI$$



**Figure 22-28**  
**Ampère's Law and the Magnetic Field in a Solenoid**

## Magnetic Field of a Solenoid

$$B = \mu_0 \left( \frac{N}{L} \right) I = \mu_0 n I \quad (22-12)$$

SI unit: Tesla, T

Where loop density  $n = N / L$ , is the number of loops per meter length .

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### CONCEPTUAL CHECKPOINT 22–6

If you want to increase the strength of the magnetic field inside a solenoid, is it better to **(a)** double the number of loops, keeping the length the same, or **(b)** double the length, keeping the number of loops the same?

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## CONCEPTUAL CHECKPOINT 22–6

If you want to increase the strength of the magnetic field inside a solenoid, is it better to **(a)** double the number of loops, keeping the length the same, or **(b)** double the length, keeping the number of loops the same?

### Reasoning and Discussion

Referring to the expression  $B = \mu_0(N/L)I$  we see that doubling the number of loops ( $N \rightarrow 2N$ ) while keeping the length the same ( $L \rightarrow L$ ) results in a doubled magnetic field ( $B \rightarrow 2B$ ). On the other hand, doubling the length ( $L \rightarrow 2L$ ) while keeping the number of loops the same ( $N \rightarrow N$ ) reduces the magnetic field by a factor of 2 ( $B \rightarrow B/2$ ). Hence, to increase the field one should pack more loops into the same length.

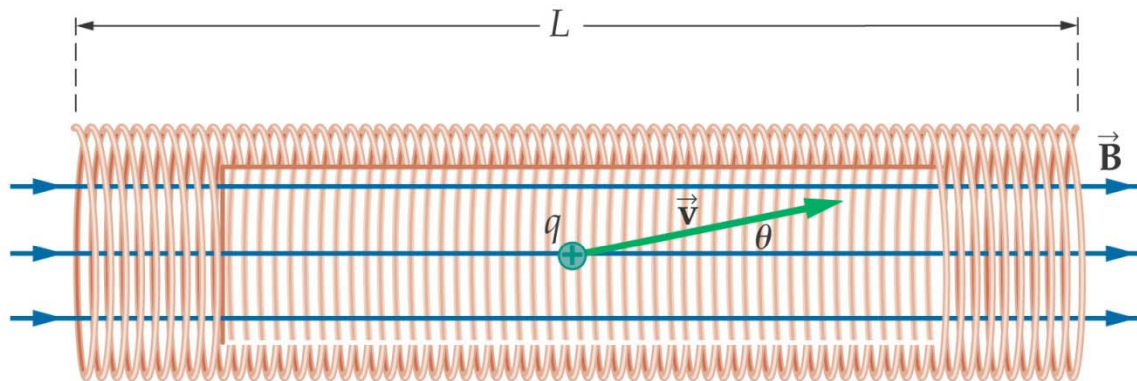
### Answer:

**(a)** Double the number of loops with the same length.

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### Example 22-7 Through the Core of a Solenoid

A solenoid is 20.0 cm long, has 200 loops, and carries a current of 3.25 A. Find the magnitude of the force exerted on a 15.0  $\mu\text{C}$  charged particle moving at 1050 m/s through the interior of the solenoid at angle of  $11.5^\circ$  to the solenoid axis.



### Example 22-7 Through the Core of a Solenoid

## Summary

(Uniform) Magnetic Field of a Solenoid

$$B = \mu_0 \left( \frac{N}{L} \right) I = \mu_0 n I \quad (22-12)$$

SI unit: Tesla, T